First-principles study of ternary hydrides for solid state hydrogen storage

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Solid state storage of hydrogen is a promising step for the ongoing energy transition. In this paper, we perform first-principles calculations on a selection of crystals using Quantum Espresso. The selection of crystals consists of ternary hydrides containing an alkali metal and aluminum (AM-Al-H), with some additional calculations for Li-B-H. The selection of structures is made, based on convex hull crystals of the Na-Al-H category ternary phase diagram with AlH₃ and NaH as endmembers. Based on our calculations, the most suitable ternary hydrides are found to be Li_3AlH_6 and $LiBH_4$ mainly based on hydrogen density, weight percentage and formation energies of endmembers. The post-processing codes can be found in this GitHub repository MS_Project https://github.com/HuangJiaLian/MS_Project.

Keywords: hydrogen storage, density functional theory

I. Introduction

H ydrogen as an energy carrier is very interesting because of its (potentially) non-polluting nature and high energy per mass (almost 3x more than diesel [1]). However, its storage remains one of the critical problems that prohibit the implementation [2]. Under standard conditions, a liter of hydrogen gas will only provide around 0.003 kWh while the same volume of diesel holds around 3 kWh [1].

By thinking of the ideal gas law, it is easy to see that increasing the pressure or lowering the temperature will also increase the volumetric density. However, the safety of storing a flammable gas under high pressure is concerning regarding safety [3, 4] and liquification of hydrogen is generally not economic [3]. These factors make it interesting to research solid state storage. The focus of this paper is mainly on ternary hydrides containing an alkali metal and aluminum, based on Na-Al-H structures. Additionally, crystals of the form Li-B-H were studied. In section II. of this paper, our methods for choosing suitable crystals are explained, and the technical data of the calculations is given. Next, in section III., the results are shown and discussed. At last, the content of this paper is summarized in section IV..

II. Methods and Material

Density functional theory (DFT) [5, 6] calculations were conducted using Quantum Espresso (QE) [7, 8] with Perdew-Burke-Ernzerhof (PBE) exchange correlation functional [9] for generalized gradient approximation (GGA). The standard solid-state pseudopotentials (SSSP) library (PBE Efficiency v1.3.0) [10] was used. The Atomic Simulation Environment (ASE) [11, 12] and pymatgen [13] are used to process the CIF files. The bilbao website [14–16] is used to determine the degree of freedom. The basis set size for the wave functions (ecutwfc), the basis set size for the density (ecutrho), and the K-points in reciprocal space were determined by convergence testing using the minimum precision of 3 mRy/au in forces and 3 kbar for any component of the stress tensor as the criteria.

The following types of ternary hydrides were investigated: XH, XAlH₄, X₃AlH₆, X₅Al₃H₁₄ and AlH₃, with X being one of the following alkali metals: Li, Na, K, Rb or Cs. Appart from these crystals, to broaden the scope of this project, the LiB hydrides were also investigated. These were added because we wanted an interesting extension and B is very similar to Al in the periodic system. Due to the time constraint of this project, only one family containing B could be tested, so we decided to pair it to Li, the most promising alkalimetal from the previously stated groups. As an example, the Na containing hydrides are shown in their respective phase diagram in figure 1, retrieved from the Materials Project. The QE input files of the crystals were generated using cif2cell [17], based on the CIF files downloaded from the Materials Project [18]. For a given crystal there might be multiple CIF files available on the Materials Project. Therefore only the crystals with the lowest energy above convex hull prediction were used.

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Our approach involved a systematic investigation of each category of aluminum-containing alkali hydrides. Utilizing CIF files, we extracted fundamental data such as the number of atoms, geometrical degrees of freedom, hydrogen pair density, and hydrogen pressure. The initial two parameters played a significant role in accelerating the convergence testing process, with the third parameter serving as a crucial criterion for evaluating the efficacy of hydrogen storage under ideal conditions. The fourth parameter was used for comparative analysis with pressurized hydrogen gas storage systems. Specifically, the selection of the structure with the minimum number of atoms and geometrical degrees of freedom within each category facilitated efficient convergence testing. The results obtained from this testing were subsequently applied to all other structures within the same category, speeding up the overall workflow. Furthermore, these settings were used in the relaxation simulations as to create phase diagrams for every category of crystals. These phase diagrams are created in order to indicate the stability of these crystals. In the case where the formation energy of a crystal is too high (above the convex hull), it can spontaneously decompose into more stable crystals. The following generalized endmember decomposition, where X is one of the alkali metals were used for the phase diagrams:

$$(X)AlH_4 \longrightarrow AlH_3 + (X)H \tag{1}$$

$$(\mathbf{X})_{5}\mathbf{Al}_{3}\mathbf{H}_{14} \longrightarrow 3\,\mathbf{Al}\mathbf{H}_{3} + 5\,(\mathbf{X})\mathbf{H} \tag{2}$$

$$(X)_3 AlH_6 \longrightarrow AlH_3 + 3 (X)H \tag{3}$$

Note that, for the Li category of crystals the same decomposition is true for Al as well as B. It should also be noted, as previously mentioned, for every category, distinguishable by their different alkali elements, the same 4 types of crystal are used. However, not every category of crystals has those 4 types of crystal. If one or more crystals were missing, the corresponding Na type crystal was used (for all available symmetries) with the Na atoms replaced by the alkali element specific to that category. Examples will be given in the following section.

When choosing suitable crystals for hydrogen storage, it is important to establish some criteria. We are interested in increasing the volumetric density so this would be a logical first criterium. Also, as explained in the section I., the energy density per mass is a big strength of hydrogen. This will be lowered with storage in crystals so a good contender would ideally have a high weight percentage. Concretely, based on [2], we choose to put the lower limit at 9 percent.

Further, we want it to be efficient at ab- and desorption of hydrogen for the storage system to remain adequately efficient. If a large amount of energy is needed for the extraction, it wouldn't be efficient enough for real implementations. For this, we want the crystals to have formation energies on the convex hull for stability, but as close as possible to zero. In other words, there should be stability, but not so much that it hinders the application. Note that we use the formation energy



Figure 1: Ternary phase diagram for Al, Na and H, where (1) to (5) represent AlH₃, NaAlH₄, Na₅Al₃H₁₄, Na₃AlH₆ and NaH respectively. [18]

with respect to the endmembers. This gives us only an indication as opposed to a verification of the criterium. This is something we have to deal with since more complex methods (that take the exact reaction paths into account) are out of the scope of this project.

III. Results and Discussion

A. Preliminary calculations

Our investigation of alkali hydrides begins with the collection of sodium crystals, NaH, NaAlH₄, Na₃AlH₆, Na₅Al₃H₁₄, and the endmember, AlH₃. We gathered data for the number of atoms in the conventional cells of each crystal as well as their geometric degrees of freedom. The number of hydrogen atoms in the conventional cells relative to its size (as given from the CIF files) then determines the density of hydrogen and the pressure needed to obtain that density of hydrogen as a gas using the ideal gas law. For the purposes of this study, the ideal gas law gives a good approximation for the pressure. For the result of these properties, we refer to table 6 in the Appendix. This analysis was then repeated for each of the other alkali hydrides.

B. Convergence test

For the convergence test, NaAlH₄ is used as the representative for the crystal group Na-Al-H because it both has a low number of degrees of freedom (high symmetry) and also a small number of atoms. The energies and forces of each atom converged at the $5 \times 5 \times 5$ k-mesh. The choice was made to continue with a $7 \times 7 \times 7$ k-mesh, motivated by the higher accuracy and the reasonable increase in computational cost. We could have also chosen a non-symmetrical k-mesh (e.g. $5 \times 5 \times 3$), since this represents the ratio between the lattice parameters better. However, we have access to sufficient computing resources and since the same parameters are used for the endmembers (which are cubic), it made more sense to keep the

| Crystal group | k-mesh | ecutwfc | ecutrho |
|---------------|--------------------------|---------|---------|
| Li-Al-H | $5 \times 5 \times 5$ | 70 | 200 |
| Na-Al-H | $7 \times 7 \times 7$ | 70 | 280 |
| K-Al-H | $15 \times 15 \times 15$ | 60 | 240 |
| Rb-Al-H | $5 \times 5 \times 5$ | 50 | 250 |
| Cs-Al-H | $7 \times 7 \times 7$ | 80 | 400 |
| Li-B-H | $7 \times 7 \times 7$ | 150 | 600 |

Table 1: The convergence test results for each crystal group.

k-mesh symmetrical.

Subsequently, the wave function cutoff was tested. We held a constant multiplication factor of 5 between ecutwfc and ecutrho. We tested different values in steps of 10 for the ecutwfc. We observed sufficient convergence at ecutwfc = 70. We kept the 7x7x7 kmesh and ecutwfc = 70 and varied the multiplication factor. Here it was found that a factor of 4 adequate convergence). The general convergence testing results are given in Table 1.

C. Structure relaxation results and hydrogen density

After retrieving the above settings, these were used in the relaxation simulations for the atomic position and cell shape. From these simulations, the H₂ densities, weight percentages (of the hydrogen) and ideal gas equivalent pressures were calculated. The results are shown in Table 2, together with the number of atoms and the space group. As written in section II., for hydrogen storage, both high H₂ density and weight percentage are desirable. Using this criterion exclusively, the Li-B-H and Li-Al-H category crystals make the best hydrogen storage materials. It also becomes clear that if the same amount of hydrogen gas were to be stored without the use of crystals, the pressure would be very high.

More specifically, still purely based on these criteria, the most interesting ternary hydrides are the ones in the Li-B-H and Li-Al-H families. All the others don't have adequate weight percentages. The binary hydrides AlH₃, LiH and BH₃ are also interesting, but we can't apply the other criteria on them since they themselves are the reference energies. With the unknown reaction paths for hydrogen desorption, this is a limitation we have to deal with for this study.

D. Formation energies

The next essential criterion that is investigated is the stability of the crystals. To this end, the phase diagrams of X-Al-H category crystals are shown in Figure 2. The formation energies of these crystals are shown in Table 3. From the Li-Al-H phase diagram, Figure 2(a) it becomes clear that LiAlH₄ and Li₅Al₃H₁₄ are unstable and therefore not wanted for hydrogen storage. In general, all crystals of the form $X_5Al_3H_{14}$ are unstable, except for Na₅Al₃H₁₄. However, this could be due to the lack of CIF files in the databases,



Figure 2: Phase diagrams for crystal group Li-Al-H, Na-Al-H, K-Al-H, Rb-Al-H and Cs-Al-H.

which makes us base the structures on $Na_5Al_3H_{14}$. Therefore these crystals do not necessarily have the symmetry with the lowest energy and thus the most stable configuration. In other words the crystal might have ended up in local energy minimum instead of a global energy minimum during the relaxation. The phase diagram of the Li-B-H category crystals is shown in Figure 3 and the formation energies in Table 5. From those, it is clear that only LiBH₄ passes the stability criterium. However, it may be too stable in the sense that the extraction of hydrogen could possibly require too much energy. As stated in section II., the verification of this is out of the scope of this study so a definitive conclusion can not be made.

In conclusion, from the available indicators and chosen crystals in this study, the most suitable ternary hydrides are found to be Li_3AlH_6 and LiBH_4 . Their properties are listed once again in table 4. From this it is clear that Li_3AlH_6 is preferred when the emphasis is on the crystal having a low formation energy, but LiBH_4 is when focusing on maximizing the H₂ density and weight percentage, regardless of formation energy.

IV. Summary

To summarize, using first-principles calculations with a minimum precision of 3 mRy/au in forces and 3 kbar for any component of the stress tensor, numerous ternary hydrides were tested. Some criteria for the selection of useful candidates were established, regarding stability, the volumetric H_2 density and weight

| Crystal | # Atoms | Spacegroup | H_2 density $[Å^{-3}]$ | Weigth percentage [%] | Pressure [atm] |
|--|---------|-------------|--------------------------|-----------------------|----------------|
| $\operatorname{AlH}_3^{[19]}$ | 64 | F d -3 m | 0.0322 | 10.08 | 1286 |
| $\mathrm{Li}_{3}\mathrm{AlH}_{6}^{[20]}$ | 60 | P -3 | 0.0343 | 11.23 | 1370 |
| ${\rm Li}_5 {\rm Al}_3 {\rm H}_{14} * ^{[21]}$ | 44 | P 4/m n c | 0.0375 | 10.87 | 1498 |
| $LiAlH_4^{[22]}$ | 24 | P 2/c | 0.0373 | 10.62 | 1489 |
| $LiH^{[23]}$ | 8 | F m -3 m $$ | 0.031 | 12.68 | 1239 |
| $Na_3AlH_6^{[24]}$ | 20 | P 21/c | 0.026 | 5.93 | 1039 |
| $Na_5Al_3H_{14}^{[21]}$ | 44 | P 4/m n c | 0.0296 | 6.72 | 1183 |
| $NaAlH_4^{[25]}$ | 24 | I 41/a | 0.0286 | 7.47 | 1143 |
| $NaH^{[26]}$ | 8 | F m -3 m $$ | 0.0177 | 4.2 | 707 |
| $K_{3}AlH_{6}^{[27]}$ | 20 | P 21/c | 0.0192 | 4.02 | 767 |
| $K_5Al_3H_{14}^{*[21]}$ | 44 | P 4/m n c | 0.0232 | 4.86 | 926 |
| $\mathrm{KAlH}_4^{[28]}$ | 24 | P n m a | 0.0218 | 5.75 | 871 |
| $KH^{[29]}$ | 2 | F m -3 m $$ | 0.0109 | 2.51 | 434 |
| $\mathrm{Rb}_3\mathrm{AlH}_6{}^{*[24]}$ | 20 | P 21/c | 0.0171 | 2.09 | 682 |
| $Rb_5Al_3H_{14}^{*[21]}$ | 44 | P 4/m n c | 0.0206 | 2.7 | 822 |
| $RbAlH_4^{[30]}$ | 24 | P n m a | 0.0186 | 3.46 | 743 |
| $RbH^{[31]}$ | 2 | F m -3 m $$ | 0.009 | 1.17 | 361 |
| $\mathrm{Cs}_{3}\mathrm{AlH}_{6}^{[32]}$ | 40 | P m -3 m | 0.015 | 1.4 | 601 |
| $Cs_5Al_3H_{14}^{*[21]}$ | 44 | P 4/m n c | 0.0184 | 1.86 | 734 |
| $\operatorname{CsAlH}_4^{[33]}$ | 24 | I 41/a m d | 0.0169 | 2.46 | 674 |
| $CsH^{[34]}$ | 8 | F m -3 m $$ | 0.0075 | 0.75 | 301 |
| $BH_{3}^{[35]}$ | 16 | P 21/c | 0.0297 | 21.86 | 1188 |
| ${\rm Li}_{3}{\rm BH}_{6}^{[36]}$ | 20 | P 1 | 0.0315 | 16.05 | 1258 |
| ${\rm Li}_5{\rm B}_3{\rm H}_{14}*^{[21]}$ | 44 | P 4/m n c | 0.0511 | 17.37 | 2039 |
| $\operatorname{LiBH}_4^{[37]}$ | 24 | P n m a | 0.037 | 18.51 | 1479 |

Table 2: Fundamental data of K, Li, Cs, Na category crystals based on the vc-relaxed output files, made with our code on GitHub. Note that the shown pressure is the ideal gas pressure equivalent. Structures that were not readily available on any of the known databases are assigned an asterisk. The CIF files of those structures were created from the Na equivalent by replacing the Na atoms with the relevant element related to the chemical formula.

| $E_{form} [eV/atom]$ | $XAlH_4$ | $X_5Al_3H_{14}$ | X_3AlH_6 |
|----------------------|----------|-----------------|------------|
| X=Li | 0.00940 | 0.00955 | -0.02322 |
| X=Na | -0.06348 | -0.06207 | -0.05635 |
| X=K | -0.12535 | -0.07825 | -0.08740 |
| X=Rb | -0.14559 | -0.06746 | -0.08929 |
| X=Cs | -0.15965 | -0.05658 | -0.10117 |

Table 3: Formation energies [eV/atom] in phase diagrams in Figure 2. The formation energy is calculated by $E_{\text{form}} = E_{\text{tot}} - n_{\text{AlH}_3} \cdot E_{\text{tot},\text{AlH}_3} - n_{\text{XH}} \cdot E_{\text{tot},\text{XH}}$, where *n* stands for the amount of times that crystal fits into the composite crystal.



Figure 3: Phase diagram with respect to BH₃-LiH. Different symmetries ([24] (sodium equivalent) and [38] (R $\overline{3}$)) were tested for Li₃BH₆ in search of a stable form, but [36] (P1) gave the least unstable result.

percentage. For the first, phase diagrams (formation energies) were used as an indicator. Combining this with an investigation of the others, we were able to point out two potential candidates for hydrogen storage. These candidates are Li_3AlH_6 and $LiBH_4$.

Note that this study is based on rather simple criteria, making our methods very efficient, but also very limited for making conclusions. The biggest weakness is in the unknown reaction paths, but the proposed candidates could still be very interesting for further research that is more dedicated on doing in-depth studies of a lower number of crystals. Such a study could also allow the binary hydrides to be considered.



Figure 4: The AlH3-NaH phase diagram before and after structure relaxation. There is not much difference between the two.

Appendix

Diagrams before and after relaxation

In addition, as an example, we compared the formation energies of the crystals in the group Na-Al-H before and after structure relaxation. This is shown in figure 4. Its results show that there was not much difference between the two. However, this does not discard relaxation as a vital step in our workflow. For starters, this being the case for the Na-Al-H category crystals does not prove other crystals also showing this behaviour. Second, leaving out the optimization might intuitively lead to distorted H_2 densities, because of the change in volume. For completeness, the total energies and formation energies before and after optimization of the Na-Al-H category crystals are shown in table 7 and table 8 respectively.

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Conflict of Interest

The authors declare no conflict of interest.

| Crystal | H_2 density $[Å^{-3}]$ | Weight percentage | Equiv. pressure [atm] | $E_{form} [eV/atom]$ |
|-------------|--------------------------|-------------------|-----------------------|----------------------|
| Li_3AlH_6 | 0.034 | 11.23 | 1370 | -0.02322 |
| $LiBH_4$ | 0.037 | 18.51 | 1479 | -0.17337 |

| Table 4: | Relevant | properties | most | suitable | crystals |
|----------|----------|------------|------|----------|----------|
| | | F F | | | |

| $LiBH_4$ | $\mathrm{Li}_{5}\mathrm{B}_{3}\mathrm{H}_{14}$ | Li ₃ BH ₆ |
|-------------------------------------|--|---------------------------------|
| -0.17337 | 0.29451 | 0.13135 |
| Li ₃ BH ₆ _R3 | Li ₃ BH ₆ _sod | |
| 0.23768 | 0.24939 | |

Table 5: Formation energies $[{\rm eV}/{\rm atom}]$ used in Figure 3.

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| Crystal | Degrees of freedom | # Atom number | H2 pairs per volume $[\mathring{A}^{-3}]$ | Pressure [atm] |
|------------------|--------------------|---------------|---|----------------|
| AlH_3 | 1 + 1 | 64 | 0.03332 | 1354.973 |
| $NaAlH_4$ | 2 + 3 | 24 | 0.02982 | 1218.516 |
| $Na_5Al_3H_{14}$ | 2 + 7 | 44 | 0.03080 | 1258.715 |
| Na_3AlH_6 | 4 + 12 | 20 | 0.02709 | 1107.229 |
| NaH | 1 + 0 | 8 | 0,01839 | 751.6966 |

Table 6: Geometrical degrees of freedom, number of atoms, H_2 density and pressure of the Na type crystals.

| | total E $[Ry]$ | total E after opt [Ry] |
|------------------|----------------|------------------------|
| AlH_3 | -172.02145099 | -172.02376572 |
| $NaAlH_4$ | -279.14766133 | -279.14800187 |
| $Na_5Al_3H_{14}$ | -1223.63600254 | -1223.64281612 |
| Na_3AlH_6 | -665.33845447 | -665.33862262 |
| NaH | -386.16160256 | -386.16264830 |

Table 7: Total energies before and after optimization of the Na-Al-H category crystals

| | $E_{\rm init}[{\rm eV/atom}]$ | $E_{\rm relax}$ [eV/atom] |
|------------------|-------------------------------|---------------------------|
| AlH ₃ | 0 | 0 |
| $NaAlH_4$ | -0,06364545 | -0,06346385 |
| $Na_5Al_3H_{14}$ | -0,06178818 | -0,06204824 |
| Na_3AlH_6 | -0,05610553 | -0,05632537 |
| NaH | 0 | 0 |

Table 8: Formation energies before and after optimiza-tion of the Na-Al-H category crystals

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